

Subject : Physics	Topic : Dual Nature of Matter and Radiation	[SOLUTIONS]
(1) (B). The de-broglie wavelength is $2\pi r_2 = 2\lambda$		
$\lambda = \pi r_2$ $r_2 = 2^2 r_1 = 4r_1 = 4 \times 0.53 = 2.12 \text{ \AA}$ $\lambda = 3.14 \times 2.12 = 6.66 \text{ \AA}$		$\Rightarrow \frac{3.32 \times 10^{-19}}{E_2} = \frac{4000}{6000}$ $\Rightarrow E_2 = 4.98 \times 10^{-19} \text{ J} = 3.1 \text{ eV.}$
(2) (C). The energy of 10 eV means that $E = eV = 10 \text{ e Volt} ; V = 10 \text{ Volt}$ The electron was accelerated through a p.d. of 10 V.		(9) (A). Slope of graph is $h/e = \text{constant}$
$\lambda = \frac{12.27}{\sqrt{V}} \text{ \AA} = \frac{12.27}{\sqrt{10}} \text{ \AA} = 3.9 \text{ \AA}$		(10) (A). $\frac{\lambda_{m_2}}{\lambda_{m_1}} = \frac{V_1}{V_2} \Rightarrow \lambda_{m_2} = \frac{6.22 \times 10^3}{10^4}$ $= 0.622 \text{ \AA}$
(3) (C). Since $W_0 = \frac{hc}{\lambda_0} \therefore \frac{(W_0)_T}{(W_0)_{Na}} = \frac{\lambda_{Na}}{\lambda_T}$		(11) (D). $\frac{E_1}{E_2} = \frac{hc}{\lambda_1} \frac{\lambda_2}{hc} = \frac{\lambda_2}{\lambda_1} \Rightarrow \frac{E_1}{E_2} = \frac{50}{1}$
or $\lambda_T = \frac{\lambda_{Na} \times (W_0)_{Na}}{(W_0)_T}$ $= \frac{5460 \times 2.3}{4.5} = 2791 \text{ \AA}$		(12) (A). Covalent bond is due to wave nature.
(4) (B). $W_0 = \frac{12375}{\lambda_0(\text{\AA})} = \frac{12375}{5420} = 2.28 \text{ eV}$		(13) (C). $\lambda = \frac{h}{\sqrt{2mE}}$
(5) (D). $W_0 = hv_0$ $\Rightarrow v_0 = \frac{W_0}{h} = \frac{2.51 \times 1.6 \times 10^{-19}}{6.6 \times 10^{-34}}$ $= 6.08 \times 10^{14} \text{ Cycle/sec.}$		(14) (A). $W_0 = hv_0 = \frac{hc}{\lambda_0}$ $\frac{(\lambda_0)K}{(\lambda_0)Na} = \frac{(W_0)Na}{(W_0)K} = \frac{2.3}{4.5} = \frac{1}{2}$
(6) (C). $W(\text{eV}) = \frac{12375}{\lambda_0(\text{\AA})}$ $\Rightarrow \lambda_0 = \frac{12375}{4.125} = 3000 \text{ \AA}$		(15) (A). $\lambda = \frac{hc}{W_0} = \frac{12420 \times 10^{-10}}{W_0(\text{eV})}$ $= \frac{12420 \times 10^{-10}}{4 \text{ eV}} = 310 \text{ nm}$
(7) (C). $P = \frac{W}{t} = \frac{nhc}{\lambda t}$ $\Rightarrow 10^3 = \frac{n \times 6.6 \times 10^{-34} \times 3 \times 10^8}{198.6 \times 1}$ $\Rightarrow n = 10^{30}$		(16) (B). Intensity $\propto \frac{1}{\text{distance}^2}$ Distance is halved intensity becomes four times, so emitted electron becomes four times.
(8) (C). $E = \frac{hc}{\lambda} \Rightarrow \frac{E_1}{E_2} = \frac{\lambda_2}{\lambda_1}$		(17) (B). $(\text{K.E.})_1 = hv_1 - hv_0$ $(\text{K.E.})_2 = hv_2 - hv_0$ As $(\text{K.E.})_1 = 2 \times (\text{K.E.})_2$ $(hv_1 - hv_0) = 2(hv_2 - hv_0)$ or $v_0 = 2v_2 - v_1$ $= 2 \times (2.0 \times 10^{16}) - (3.2 \times 10^{16})$ $= 0.8 \times 10^{16} \text{ Hz or } 8 \times 10^{15} \text{ Hz}$
		(18) (B). $W = \frac{hc}{\lambda} - K_{\max}$ $= \frac{1240}{400} - 1.68 = 1.42 \text{ eV}$

- (19) (C). Power of the bulb = 100 watt =  $100 \text{ J s}^{-1}$   
 Energy of one photon  $E = h\nu = hc/\lambda$

$$= \frac{6.626 \times 10^{-34} \text{ Js} \times 3 \times 10^8 \text{ m/s}}{400 \times 10^{-9} \text{ m}} \\ = 4.969 \times 10^{-19} \text{ J}$$

Number of photons emitted per second is

$$\frac{n}{t} = \frac{P}{E} = \frac{100 \text{ Js}^{-1}}{4.969 \times 10^{-19} \text{ J}} \\ = 2.012 \times 10^{20} \text{ s}^{-1}$$

- (20) (A). Work function,  $\phi_0 = h\nu_0$   
 where  $\nu_0$  is the threshold frequency  
 So,  $\phi_0 \propto \nu_0$ . Hence Pt > Al > K

- (21) (D). When a beam of electrons of energy  $E_0$  is incident on a metal surface kept in an evacuated chamber, electrons can be emitted with maximum energy  $E_0$  (due to elastic collision) and with any energy less than  $E_0$ , when part of incident energy of electron is used in liberating the electrons from the surface of metal.

- (22) (A). Consider an electron of mass  $m$  and charge  $e$  accelerated from rest through potential  $V$ .

$$\text{Then } K = eV ; \quad K = \frac{1}{2}mv^2 = \frac{p^2}{2m}$$

$$\therefore p = \sqrt{2mK} = \sqrt{2meV}$$

The de Broglie wavelength  $\lambda$  of the electron

$$\text{is } \lambda = \frac{h}{p} = \frac{h}{\sqrt{2mK}} = \frac{h}{\sqrt{2meV}}$$

Substituting the numerical values of  $h$ ,  $m$ ,  $e$ , we get

$$\lambda = \frac{6.63 \times 10^{-34}}{\sqrt{2 \times 9.1 \times 10^{-31} \times 1.6 \times 10^{-19} \times V}} \\ = \frac{1.227 \times 10^{-9}}{\sqrt{V}} \text{ m} = \frac{1.227}{\sqrt{V}} \text{ nm}$$

- (23) (D). Photoelectric current depends on  
 (i) the intensity of incident light.  
 (ii) the potential difference applied between the two electrodes.  
 (iii) the nature of the emitter material.

- (24) (A).  
 (i) The graph shows that the stopping potential  $V_0$  varies linearly with the frequency of incident radiation for a given photosensitive material.  
 (ii) There exists a certain minimum cut-off frequency  $\nu_0$  for which the stopping potential is zero.  
 (iii) The maximum kinetic energy of the photoelectrons varies linearly with the frequency of incident radiation, but is independent on intensity.

- (25) (B). Here,  $E = 1 \text{ MeV} = 10^6 \text{ eV}$ ,  
 $h = 6.63 \times 10^{-34} \text{ J s}$ ,  $c = 3 \times 10^8 \text{ m s}^{-1}$

$$hc = \frac{6.63 \times 10^{-34} \times 3 \times 10^8}{1.6 \times 10^{-19}} \approx 1240 \text{ eV nm}$$

$$\text{As } E = \frac{hc}{\lambda} \text{ or } \lambda = \frac{hc}{E} = \frac{1240 \text{ eV nm}}{10^6 \text{ eV}} \\ = 1.24 \times 10^{-3} \text{ nm}$$

- (26) (D).  $E_{\text{photon}} = \frac{12400}{3000} = 4.13 \text{ eV}$

Photoelectric effect can take place only if  $E_{\text{photon}} \geq \phi$

Thus, Li, Na, K, Mg can show photoelectric effect.

- (27) (B). The maximum kinetic energy of the emitted electron is given by

$$K_{\max} = h\nu - \phi_0 = h(4V) - h(V) = 3hV$$

- (28) (D).  $\frac{hc}{\lambda} - \phi = eV ; V = \frac{hc}{e\lambda} - \frac{\phi}{e}$

$$\text{For plate 1 : } \frac{\phi_1}{hc} = 0.001$$

$$\text{For plate 2 : } \frac{\phi_2}{hc} = 0.002$$

$$\text{For plate 3 : } \frac{\phi_3}{hc} = 0.004$$

$$\phi_1 : \phi_2 : \phi_3 = 1 : 2 : 4$$

For plate 2, threshold wavelength

$$\lambda = \frac{hc}{\phi_2} = \frac{hc}{0.002 hc} = \frac{1000}{2} = 500 \text{ nm}$$

For plate 3, threshold wavelength

$$\lambda = \frac{hc}{\phi_3} = \frac{hc}{0.004 hc} = \frac{1000}{4} = 250 \text{ nm}$$

Since violet colour light  $\lambda$  is 400 nm, so  $\lambda_{\text{violet}} < \lambda_{\text{threshold}}$  for plate 2  
So, violet colour light will eject photoelectrons from plate 2 and not from plate 3.

$$(29) \quad (\text{A}). \quad E_{\lambda_1}(550 \text{ nm}) = \frac{1240}{550} \text{ eV} = 2.25 \text{ eV}$$

$$E_{\lambda_2}(450 \text{ nm}) = \frac{1240}{450} \text{ eV} = 2.8 \text{ eV}$$

$$E_{\lambda_3}(350 \text{ nm}) = \frac{1240}{350} \text{ eV} = 3.5 \text{ eV}$$

For metal r, only  $\lambda_3$  is able to generate photoelectron.

For metal q, only  $\lambda_2$  and  $\lambda_3$  are able to generate photoelectron. For metal p, all wavelength are able to generate photoelectron. Hence photoelectric current will be maximum for p and least for r.

$$(30) \quad (\text{D}). \quad \frac{hc}{\lambda} = \phi + eV \quad \text{Diagram: A circle with a dot inside and an arrow pointing outwards.}$$

$$\frac{1240 \text{ (eV)} \text{ (nm)}}{200 \text{ (nm)}} = 4.7 \text{ (eV)} + \text{eV}$$

$$\frac{1240}{200} \text{ e} = 4.7 \text{ e} + \text{eV}$$

$$6.2 - 4.7 = V \quad \therefore V = 1.5 \text{ volt}$$

$$\frac{1}{4\pi\epsilon_0} \frac{Q}{R} = 1.5 ; \quad (9 \times 10^9) \frac{Ne}{\frac{1}{100}} = 1.5$$

$$9 \times 10^{11} Ne = 1.5$$

$$N = \frac{1.5}{9 \times 10^{11} \times 1.6 \times 10^{-19}} = \frac{15}{16} \times \frac{1}{9} \times 10^8$$

$$= \frac{5}{3 \times 16} \times 10^8 = \frac{50}{48} \times 10^7$$

$$\therefore Z = 7$$

$$(31) \quad (\text{C}). \quad E = \frac{hc}{\lambda}$$

$$\Rightarrow E = \frac{12375}{\lambda \text{ (in } \text{\AA})} \text{ eV} \Rightarrow E = \frac{12375}{4100} \text{ eV}$$

$$\Rightarrow E \approx 3 \text{ eV}$$

$$(32) \quad (\text{C}). \quad h\nu - \phi = K_{\text{max}} = \frac{1}{2} mv_{\text{max}}^2$$

According to question,

$$\frac{5h\nu_0 - h\nu_0}{2h\nu_0 - h\nu_0} = \frac{v_2^2}{v_1^2}$$

$$v_2 = 2v_1 = 2 \times 4 \times 10^6 = 8 \times 10^6 \text{ m/s}$$

(33) (A). A photo-cell employs photoelectric effect to convert light energy into photoelectric current.

(34) (A). When electrons emitted from cathode collide with gas molecules atoms, they knock out outer electrons and produce positively charged ions. They become part of positive ray.

$$(35) \quad (\text{C}). \quad 1 \text{ MeV} = 10^6 \times 1.6 \times 10^{-19} \text{ joule}$$

$$\text{Momentum of photon} = \frac{E}{c} = \frac{1.6 \times 10^{-13}}{3 \times 10^8}$$

$$= \frac{1.6}{3} \times 10^{-21} = \frac{16}{3} \times 10^{-22}$$

$$= 5 \times 10^{-22} \text{ kg m/sec.}$$

$$(36) \quad (\text{D}). \quad \text{Since } p = \frac{n\hbar v}{t}$$

$$\Rightarrow \frac{n}{t} = \frac{p}{\hbar v} = \frac{2 \times 10^{-3}}{6.6 \times 10^{-34} \times 6 \times 10^{14}}$$

$$= 5 \times 10^{15}$$

(37) (D). Number of emitted electrons

$$N_E \propto \text{Intensity} \propto \frac{1}{(\text{Distance})^2}$$

Therefore, as distance is doubled,  
 $N_E$  decreases by (1/4) times.

$$(38) \quad (\text{A}). \quad KE_{\text{max}} = h\nu - \phi$$

or  $h\nu = KE_{\text{max}} + \phi = 5 \text{ eV} + 6.2 \text{ eV} = 11.2 \text{ eV}$

$$\lambda = \frac{12420 \times 10^{-10}}{11.2 \text{ (eV)}}$$

$\approx 1000 \text{ \AA}$  which is in ultraviolet region.

- (39) (B).  $m_e v_e = mv$

$$v = \frac{m_e v_e}{m} = \frac{9.1 \times 10^{-31} \times 3 \times 10^6}{10^{-6}} \\ = 2.7 \times 10^{-18} \text{ m/s}$$

- (40) (B). Saturation current  $\propto$  intensity

- (41) (A). Curves (a) & (b) represent incident radiations of same frequency but of different intensities.

- (42) (A).  $\lambda = 667 \times 10^{-9} \text{ m}$ ,  $P = 9 \times 10^{-3} \text{ W}$

$$P = \frac{Nhc}{\lambda}, N : \text{No. of photons emitted/sec.}$$

$$N = \frac{9 \times 10^{-3} \times 667 \times 10^{-9}}{6.6 \times 10^{-34} \times 3 \times 10^8} \\ = \frac{9 \times 6.67 \times 10^{-10}}{3 \times 6.6 \times 10^{-26}} \approx 3 \times 10^{16} / \text{sec}$$

- (43) (D), (44) (D).

$$\phi_A = \frac{13.6}{4} \text{ eV}, \phi_B = \frac{13.6 \times 4}{4} \text{ eV}$$

$$E - \phi_A = (KE)_A, E - \phi_B = (KE)_B$$

$$KE_A = 2KE_B; E - \phi_A = 2(E - \phi_B)$$

$$E = 2\phi_B - \phi_A = 2 \times 13.6 - \frac{13.6}{4} = 23.8 \text{ eV}$$

- (45) (D). Einstein P.E. equation

$$\text{Case I : } eV = \frac{hc}{\lambda} - \frac{hc}{\lambda_0} \quad \dots \dots (1)$$

**Case II :**

$$e \frac{V}{4} = \frac{hc}{2\lambda} - \frac{hc}{\lambda_0} \Rightarrow eV = \frac{4hc}{2\lambda} - \frac{4hc}{\lambda_0} \quad \dots \dots (2)$$

Eq. (1) – eq. (2)

$$\frac{hc}{\lambda} - \frac{2hc}{\lambda} = -\frac{4hc}{2\lambda} + \frac{hc}{\lambda_0} \Rightarrow \frac{hc}{\lambda} = -\frac{3hc}{\lambda_0} \Rightarrow \lambda_0 = 3\lambda$$